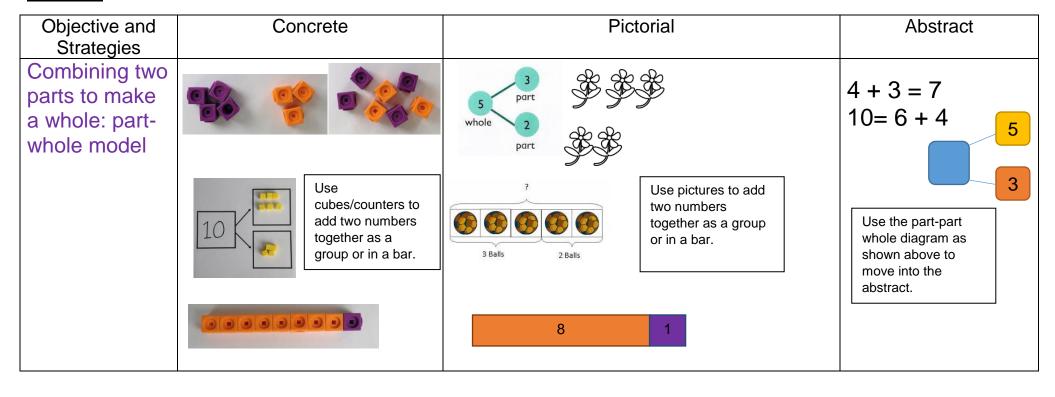
The Teaching of Maths at Bramhope Primary School (Working document)

At Bramhope Primary School, we have a mastery approach to the teaching of maths. The aim of this is for pupils to develop conceptual understanding alongside procedural fluency. The use of practical apparatus to support the understanding of number and calculation is being embedded across school and this, along with clear calculation guidelines, ensures that pupils are moved through **concrete**, **pictorial** and **abstract** representations in a planned sequence and at an appropriate pace. If you would like to find out more about the mastery approach, please do talk to your child's class teacher.

Progression in Calculations

Addition



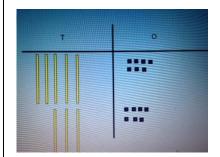
Starting at the bigger number and counting	(*************************************	12 + 5 = 17	5 + 12 = 17
on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10.	6 + 5 = 11	Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10? How many more do I add on now?
	Start with the bigger number and use the smaller number to make 10. (Tens frame)	9 + 5 = 14 1 4 +1 0 1 2 3 4 5 6 7 8 9 (10) 11 12 13 (14) 15 16 17 18 19 20	
Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make		4+7+6 = 10+7 = 17 Combine the two numbers that make 10 and then add on the remainder.
	10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	

Partitioning and recombining	3 + 5 + 3 = 11 Look for a double and add on the third digit. Using Numicon and Base 10	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	24 = 20 + 4 13 = 10 + 3 30 + 7 = 37 Ongoing dialogue which is not necessary to record
		Partitioning 28 + 39 28 + 39 50 + 17 = 67	28 = 20 + 8 39 = 30 + 9 50 + 17 = 67 Ongoing dialogue which is not necessary to record

		Jotting alongside use of apparatus	
Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters. T O O O O O O O O O O O O O O O O O O	After practically using the Base 10 blocks and place value counters, children can draw sticks and dots to represent the Base 10 blocks or the counters to help them to solve additions. 32 + 23 = T O T O T O T O T O T O T O T O T O T	<u>Calculations</u> 21 + 42 = 21 + <u>42</u>

Column methodregrouping

Make both numbers on a place value grid using Base 10 rods and cubes.

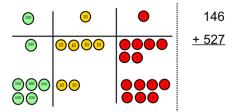


57 +37

Add the ones and exchange 10 ones for a 10 stick

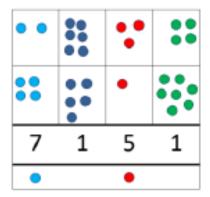


Using place value counters



Add up the ones and exchange 10 ones for one 10.

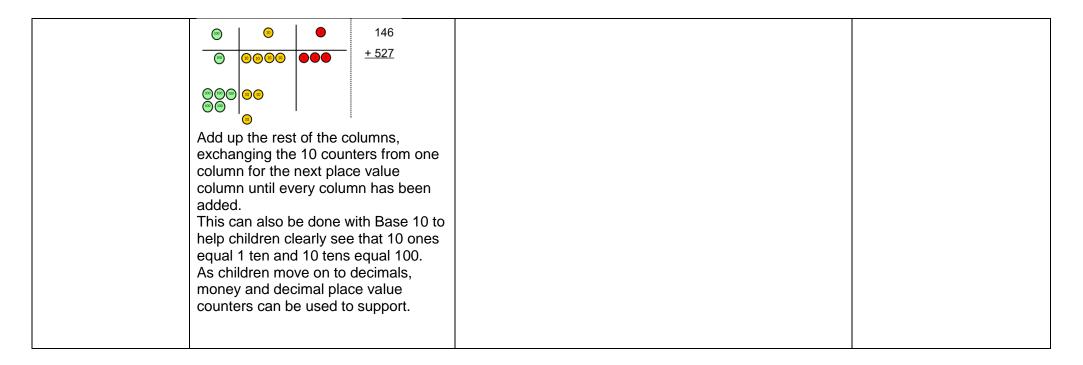
Children can draw a pictoral representation of the columns and Base 10/place value counters to further support their learning and understanding.



Show the exchange below the addition.

57 +37

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

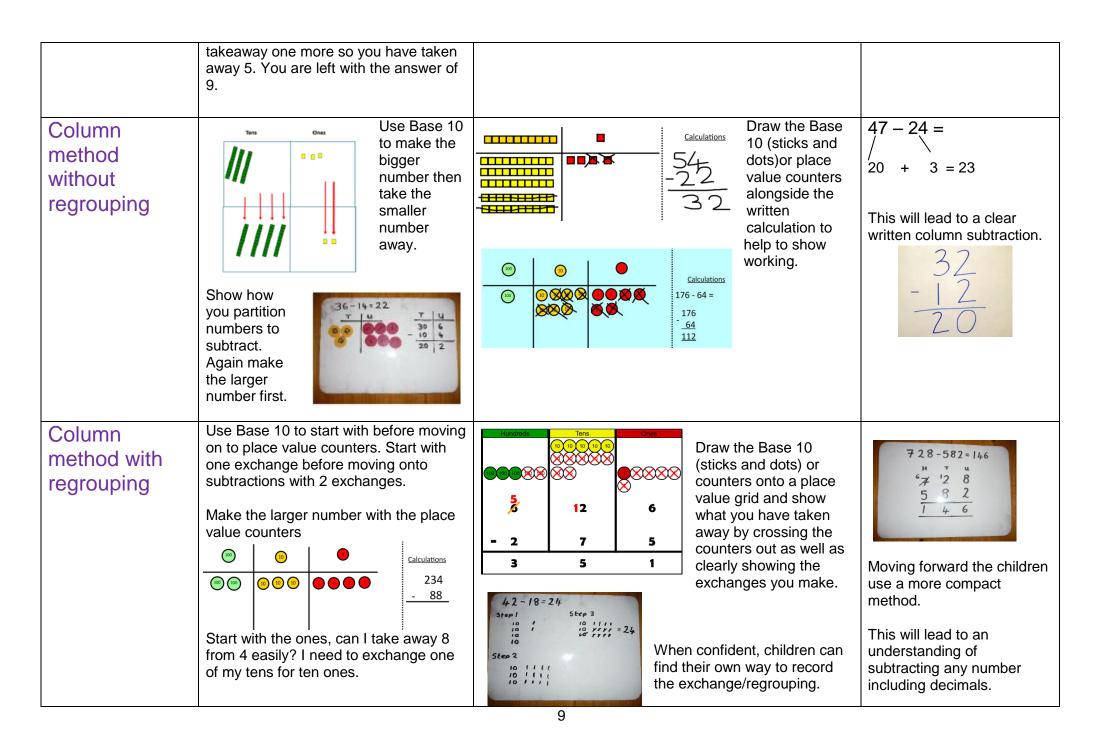


Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-2=4$	Cross out drawn objects to show what has been taken away.	18 - 3= 15 8 - 2 = 6 = 17 - 4

	4-2=2		
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. 57 – 23 =	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Use counters and move them away from the group as you take them away counting backwards as you go.	This can progress all the way to counting back using two 2 digit numbers.	

Find the difference	Compare amounts and objects to find the difference. Use cubes to build towers or make bars to find the difference Use basic bar models with items to find the difference	Count on to find the difference. Comparison Bar Models Draw bars to find the difference in age between them. Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them. 13 ? Lisa Sister	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches.
Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 – 6 =	Use a pictorial representation of objects to show the part part whole model.	Move to using numbers within the part whole model.
Make 10	14 – 5 = Make 14 on the ten frame. Take away the four first to make 10 and then	13 - 7 = 6 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the previous 10? How many do we have left to take off?



-		234 ch	ust writing the numbers as shown here shows that the hild understands the method and knows when to schange/regroup.	- 2	5 12 6 3 2 6 3 6		
	Now I can subtract my ones.			2	3 0	•	
		Calculations 234 - 88					
	Now look at the tens, can I take tens easily? I need to exchange hundred for ten tens.	away 8 one					
		234 - 88					
	Now I can take away eight tens complete my subtraction	and					
		Calculations 734 - 88 146					
	Show children how the concrete method links to the written meth alongside your working. Cross on numbers when exchanging and where we write our new amount	od out the show					

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number. Double 4 is 8	16 10 6 12 20 12 Partition a number and then double each part before
Counting in			recombining it back together. Count in multiples of a
Counting in multiples		Sus out Sus out Sus out	number aloud. Write sequences with multiples of numbers.
		0 5 10 15 20 25 30	2, 4, 6, 8, 10
	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	5, 10, 15, 20, 25 , 30

Repeated addition



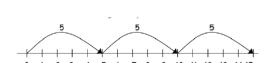




Write addition sentences to describe objects and pictures.



Use different objects to add equal groups.



2 add 2 add 2 equals 6

5 + 5 + 5 = 15

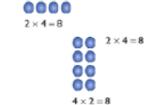


Arraysshowing commutative multiplication Create arrays using counters/ cubes to show multiplication sentences.





Draw arrays in different rotations to find **commutative** multiplication sentences.



0000 4×2=8

Link arrays to area of rectangles.

Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

$$3 + 3 + 3 + 3 + 3 = 15$$

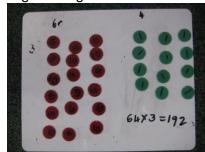
$$5 \times 3 = 15$$

$$3 \times 5 = 15$$

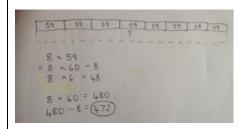
Column multiplication

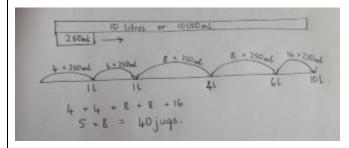
Children can continue to be supported by place value counters at the stage of multiplication.

2 digit x 1 digit



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.





Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

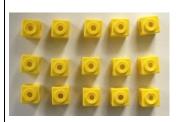
If it helps, children can write out what they are solving next to their answer.

	This moves to the more compact method.
	3 6 5 2 X 8
	2 9 2 1 6
	2 3 1
	1342
	x 18
	13420
	10736
	24156
	Multiplication of decimals: money/measures
	3. 1 9 X 8
	25. 5 2

Division

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
	96 ÷ 3 = 32	be within each group. $ \begin{array}{c} 20 \\ ? \\ 20 \div 5 = ? \\ 5 \times ? = 20 \end{array} $	

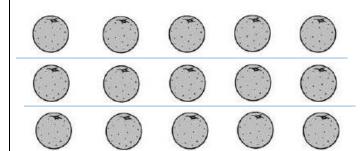
Division within arrays



Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

Eq $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$



Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Jump forward in equal jumps on a number line then see

how many more you need to jump to find a remainder.

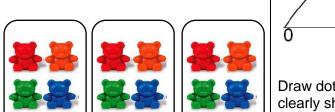
Find the inverse of multiplication and division sentences by creating four linking number sentences.

 $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$

Division with a remainder



Divide objects between groups and see how much is left over



Complete written divisions and show the remainder using r.

 $29 \div 8 = 3 \text{ REMAINDER 5}$

Draw dots and group them to divide an amount and clearly show a remainder.











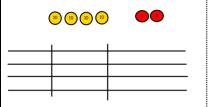




Short division

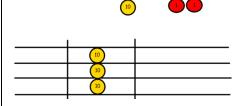
Use place value counters to divide using the bus stop method alongside

Calculations
42 ÷ 3



 $42 \div 3 =$

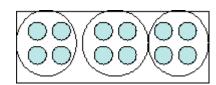
Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



We exchange this ten for ten ones and then share the ones equally among the groups.

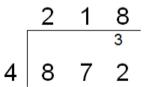
We look how much in 1 group so the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.



Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.

or 663 5/8

or 663.6

		Divisions should be given in real life contexts, including money and measures, so that pupils know to round the answer up or down.